

The Solid State

Structure Types of A_NB_M Solids

The crystal structure of the elements

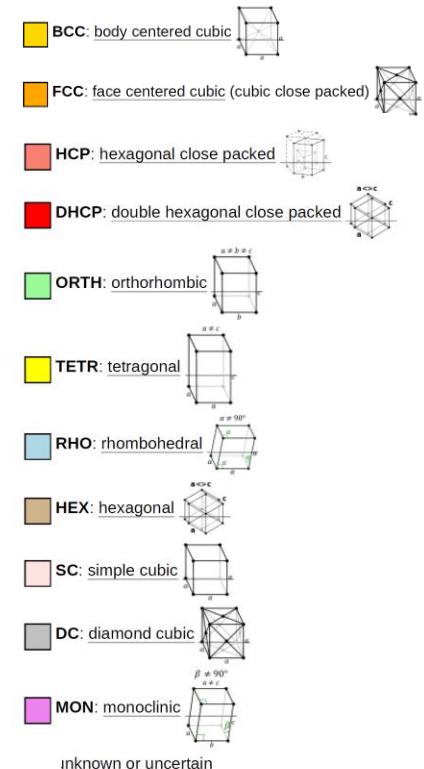
Crystal structure of elements in the periodic table																	
1 H HEX																	2 He HCP
3 Li BCC	4 Be HCP																
11 Na BCC	12 Mg HCP																
19 K BCC	20 Ca FCC	21 Sc HCP	22 Ti HCP	23 V BCC	24 Cr BCC	25 Mn BCC	26 Fe BCC	27 Co HCP	28 Ni FCC	29 Cu FCC	30 Zn HCP	31 Ga ORTH	32 Ge DC	33 As RHO	34 Se HEX	35 Br ORTH	36 Kr FCC
37 Rb BCC	38 Sr FCC	39 Y HCP	40 Zr HCP	41 Nb BCC	42 Mo BCC	43 Tc HCP	44 Ru HCP	45 Rh FCC	46 Pd FCC	47 Ag FCC	48 Cd HCP	49 In TETR	50 Sn TETR	51 Sb RHO	52 Te HEX	53 I ORTH	54 Xe FCC
55 Cs BCC	56 Ba BCC	57* La DHCP	72 Hf HCP	73 Ta BCC/TETR	74 W BCC	75 Re HCP	76 Os HCP	77 Ir FCC	78 Pt FCC	79 Au FCC	80 Hg RHO	81 Tl HCP	82 Pb FCC	83 Bi RHO	84 Po SC/RHO	85 At [FCC]	86 Rn FCC
87 Fr [BCC]	88 Ra BCC	89** Ac FCC	104 Rf [HCP]	105 Db [BCC]	106 Sg [HCP]	107 Bh [FCC]	108 Hs [BCC]	109 Mt [BCC]	110 Ds [BCC]	111 Rg [BCC]	112 Cn [HCP]	113 Nh [HCP]	114 Fl [HCP]	115 Mc [FCC]	116 Lv [FCC]	117 Ts [HCP]	118 Og [FCC]
* 58 Ce DHCP/FCC 59 Pr DHCP 60 Nd DHCP 61 Pm DHCP 62 Sm RHO 63 Eu BCC 64 Gd HCP 65 Tb HCP 66 Dy HCP 67 Ho HCP 68 Er HCP 69 Tm HCP 70 Yb FCC 71 Lu HCP																	
** 90 Th FCC 91 Pa TETR 92 U ORTH 93 Np ORTH 94 Pu MON 95 Am DHCP 96 Cm DHCP 97 Bk DHCP 98 Cf FCC 99 Es FCC 100 Fm [FCC] 101 Md [FCC] 102 No [FCC] 103 Lr [HCP]																	

	nonmetal structures	closest-packings of spheres [†]	body-centered cubic	other metal structures
nonmetals*				
ambient pressure	55	4‡	—	—
high pressure	4	8	7	31
metals				
up to 400 K	2	51	15	11
high temperature	—	7	23	6
high pressure	—	31	8	39
total	61	101	53	87

* including Si, Ge, As, Sb, Te. All temperature ranges

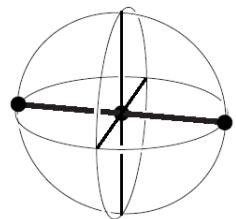
† including slightly distorted variants

‡ noble gases

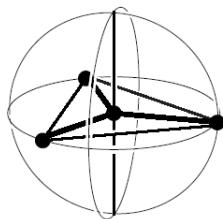


The crystal structure of molecules

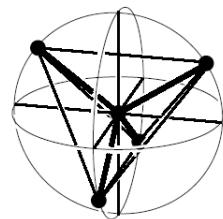
VSEPR and Bond-Valence theory



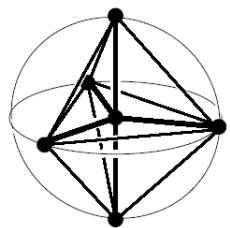
2
linear arrangement



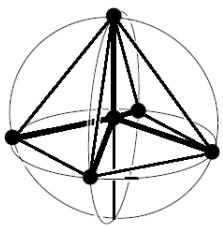
3
triangle



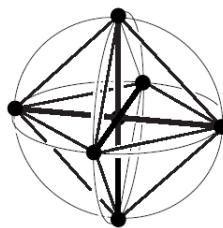
4
tetrahedron



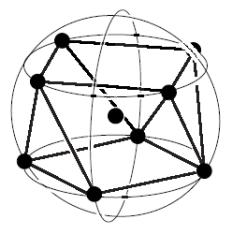
5 = 2 + 3
trigonal bipyramidal



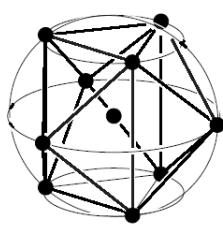
5 = 1 + 4
square pyramidal



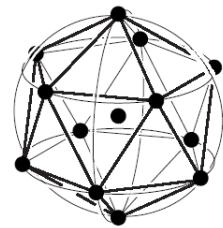
6
octahedron



8
square
antiprism



9 = 6 + 3
triply capped
trigonal prism

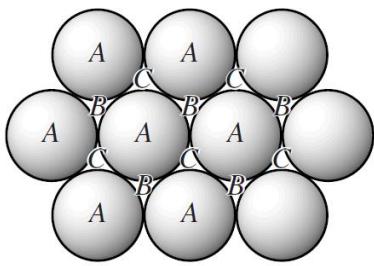


12
icosahedron

composition	structure	angle XAX	examples
AX_2E		$< 120^\circ$	$\text{SnCl}_2(\text{g}), \text{GeBr}_2(\text{g})$
AX_2E_2		$< 109,5^\circ$	$\text{H}_2\text{O}, \text{F}_2\text{O}, \text{Cl}_2\text{O}, \text{H}_2\text{S}, \text{H}_2\text{N}^-$
AX_2E_3		180°	$\text{XeF}_2, \text{I}_3^-$
AX_3E		$< 109,5^\circ$	$\text{NH}_3, \text{NF}_3, \text{PH}_3, \text{PCl}_3, \text{OH}_3^+, \text{SCI}_3^+, \text{SnCl}_3^-$
AX_3E_2		$< 90^\circ$	ClF_3
AX_4E		$< 90^\circ$ and $< 120^\circ$	SF_4
AX_4E_2		90°	$\text{XeF}_4, \text{BrF}_4^-, \text{ICl}_4^-$
AX_5E		$< 90^\circ$	$\text{SbCl}_5^{2-}, \text{SF}_5^-, \text{BrF}_5$
AX_5E_2		72°	XeF_5^-

The crystal structure of the metals

Hard-sphere model



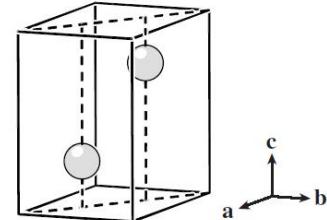
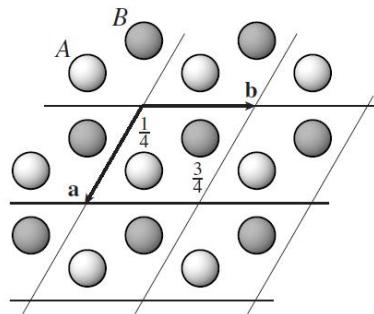
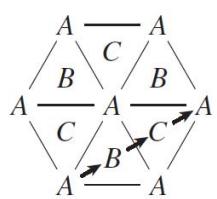
$$SF = \frac{4\pi}{3V} \sum_i Z_i r_i^3 \quad (14.1)$$

V = volume of the unit cell

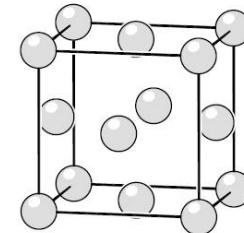
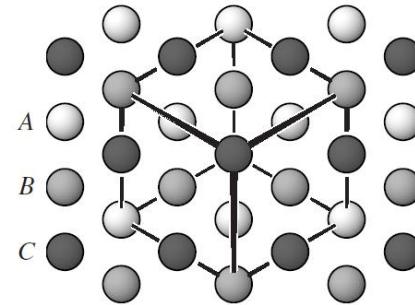
r_i = radius of the i -th kind of sphere

Z_i = number of spheres of the i -th kind
in the unit cell

Closest-packed spheres



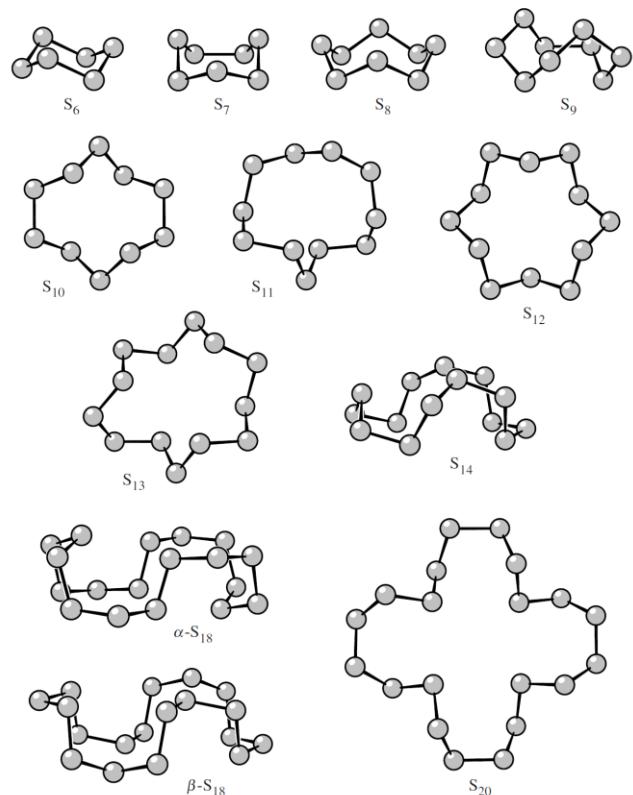
$P6_3/mmc$ $c/a = \frac{2}{3}\sqrt{6} = 1.633$
Wyckoff position $2d$ $\frac{2}{3}, \frac{1}{3}, \frac{1}{4}$



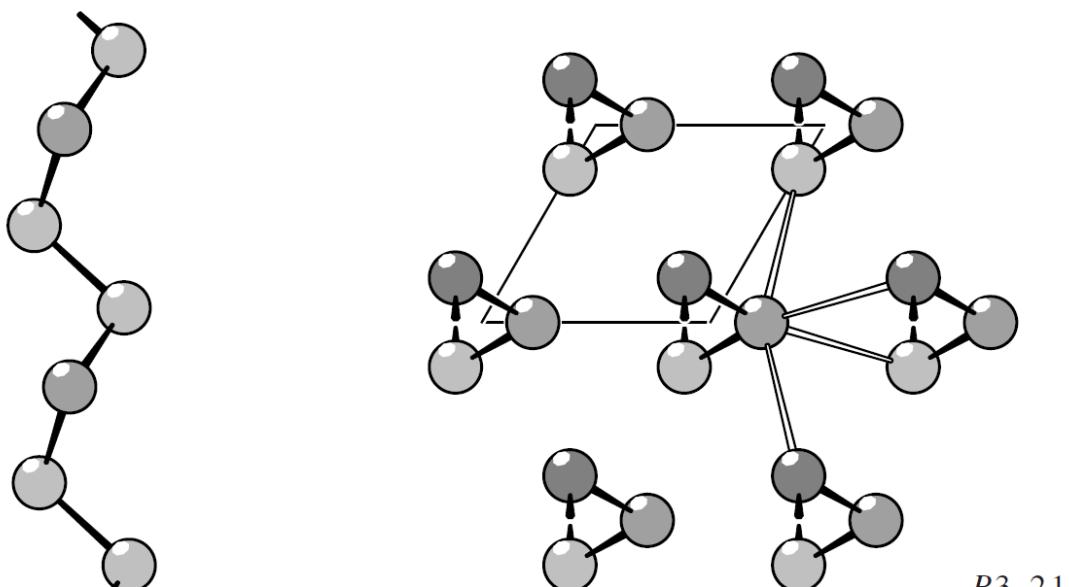
$Fm\bar{3}m$
 $4a$ $0, 0, 0$

The crystal structure of the nonmetals

Sulfur



Tellurium



AB Structures

- There are 5 principal structures with AB stoichiometry
- Most common:
 1. Rock salt or NaCl-type (6-coord)
 2. CsCl-type (8-coord)
 3. Zinc Blende or ZnS (4-coord)
 4. Wurtzite or ZnS (4-coord)
 5. NiAs-type (6-coord)

AB Structures

- 1. PbO-type
- 2. SnS-type
- 3. TlI-type
- 4. HgS-type
- 5. PtS-type
- 6. GaS-type
- 7. BN-type
- 8. CuS-type
- 9. NiTe-type
- 10. AuSe

What determines a structure?

- Ionic compounds: CaF_2
- Covalent compounds: MoS_2 , FeS_2
- In ionic compounds, size considerations determine structure.
- In covalent compounds, size considerations are also important, but there are more exceptions.

Binary Compounds (Phases)

- AB
- AB_2
- AB_3
- A_2B_3
- A_xB_y
- Zintl Phases

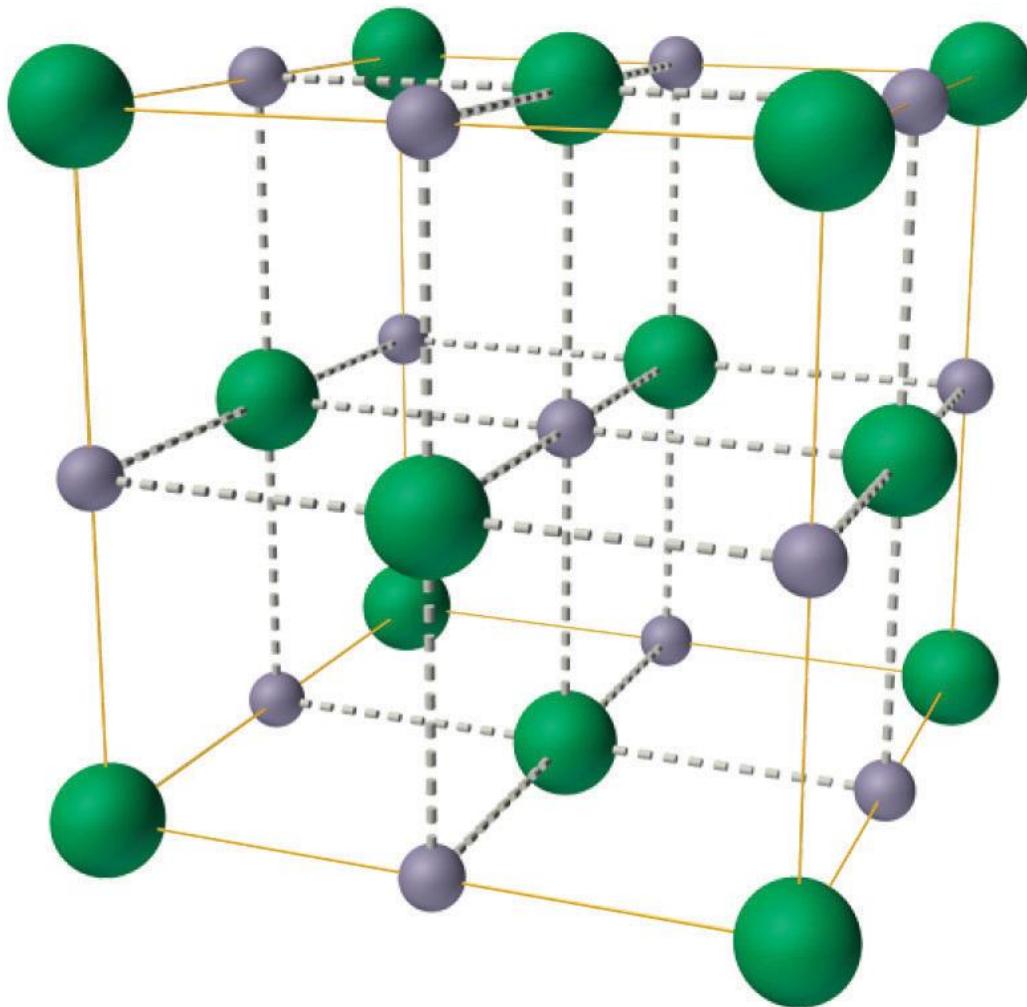
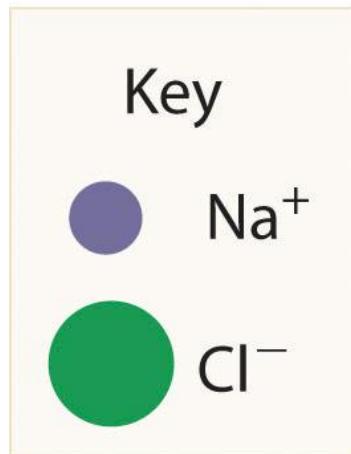
*Although sometimes used interchangeably, ‘phase’ and ‘compound’ are not entirely synonymous

Ternary Compounds (Phases)

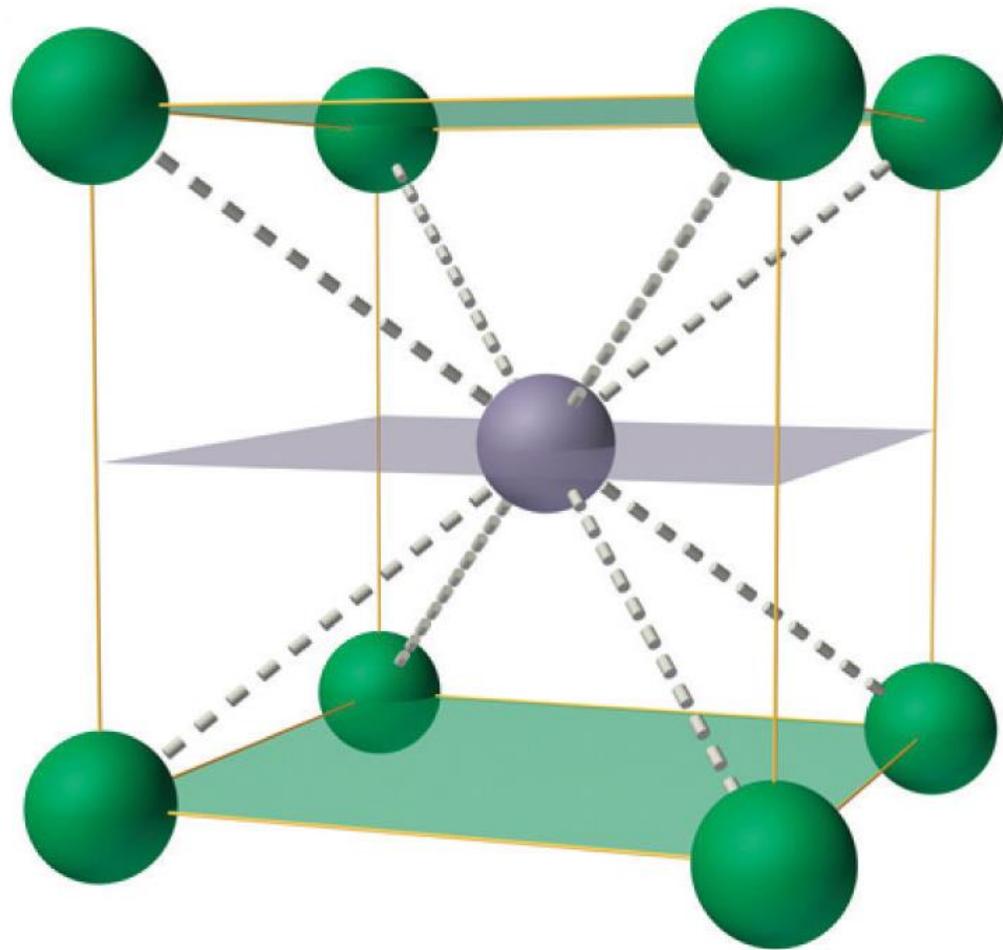
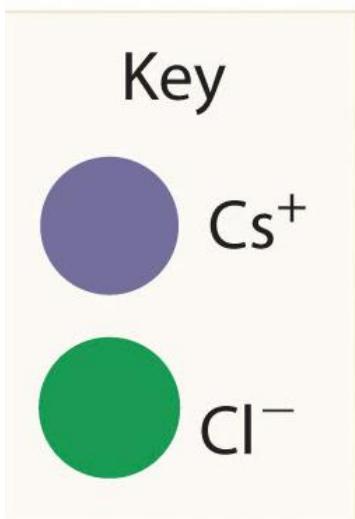
- ABX
- ABX_3
- ABX_2
- AB_2X_2
- AB_2X_4
- A_2BX_4
- $\text{A}_2\text{B}_2\text{X}_7$
- $\text{A}_3\text{B}_5\text{X}_{12}$

*Although sometimes used interchangeably, ‘phase’ and ‘compound’ are not entirely synonymous

NaCl



CsCl



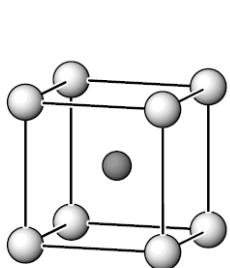
Solids

1. Ionic: NaCl
2. Covalent: GaAs
3. Metallic: Na
4. Van der Waals: naphthalene

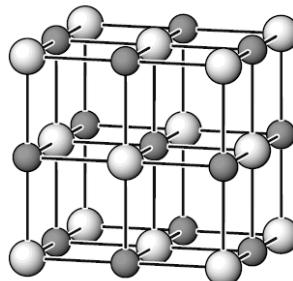
Coordination

- Rule of thumb: Small size atoms tend to have small coordination number. The opposite is true for large ions.
- Examples: NaCl CN = 6, AgI CN = 4
- Violations: LiCl CN = 6, AuI CN = 2

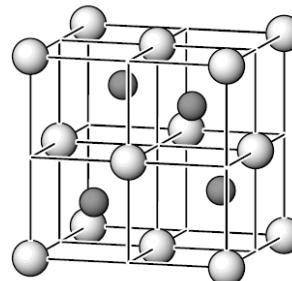
Predicting the structure-type



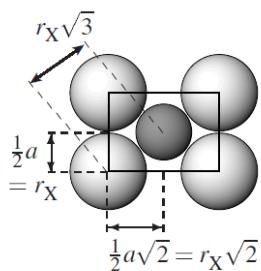
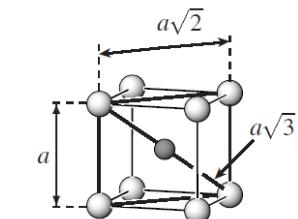
CsCl
 $Pm\bar{3}m$



NaCl
 $Fm\bar{3}m$

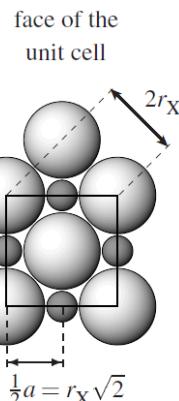


zinc blende (spahlerite, ZnS)
 $F\bar{4}3m$



CsCl type

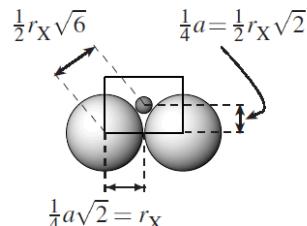
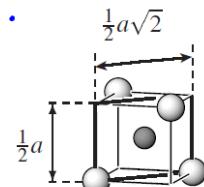
$$\begin{aligned}r_M + r_X &= r_X\sqrt{3} \\ \frac{r_M}{r_X} &= \sqrt{3} - 1 \\ &= 0.732\end{aligned}$$



NaCl type

$$\begin{aligned}r_M + r_X &= r_X\sqrt{2} \\ \frac{r_M}{r_X} &= \sqrt{2} - 1 \\ &= 0.414\end{aligned}$$

one eighth of the unit cell



zinc blende type

$$\begin{aligned}r_M + r_X &= r_X \cdot \frac{1}{2}\sqrt{6} \\ \frac{r_M}{r_X} &= \frac{1}{2}\sqrt{6} - 1 \\ &= 0.225\end{aligned}$$

Solids with the NaCl-type

MgO

TiN

Mg_6MnO_8

TiO

TiP

NaVO_4

NbO

NaLaS_2

NbN

LiAlO_2

MO (M = Transition Metal)

Solids with the CsCl-type

CsX (X = Br, I)

NH₄Cl

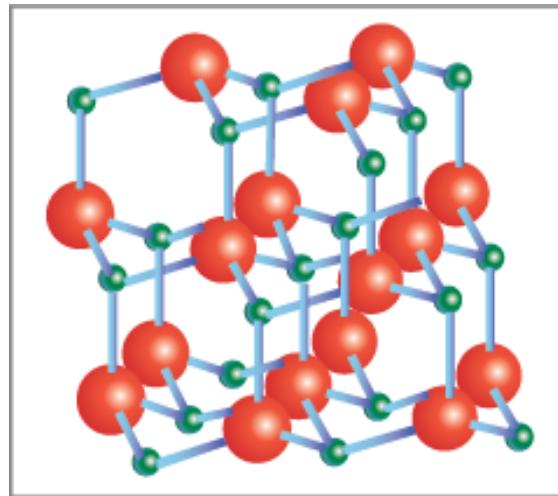
CuCN

CuSH

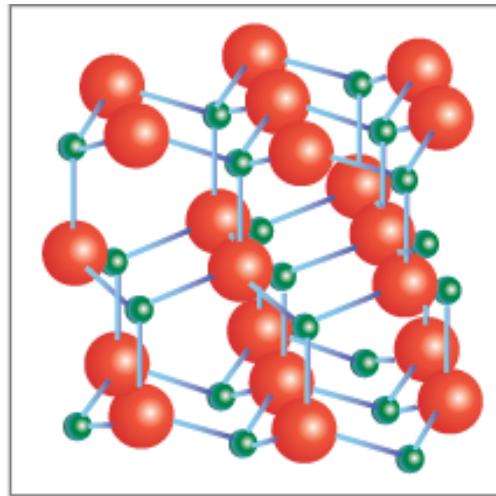
CuZn (β -brass)

AuZn

Tetrahedral Structures (Adamantine)



Zinc Blende

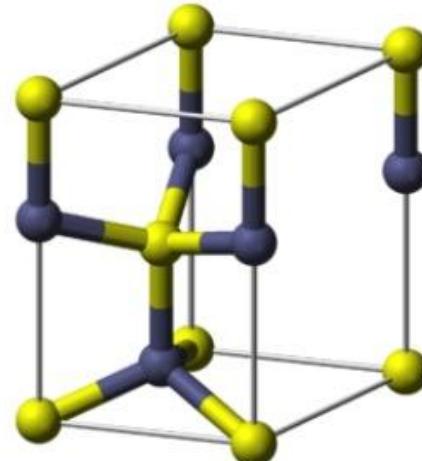
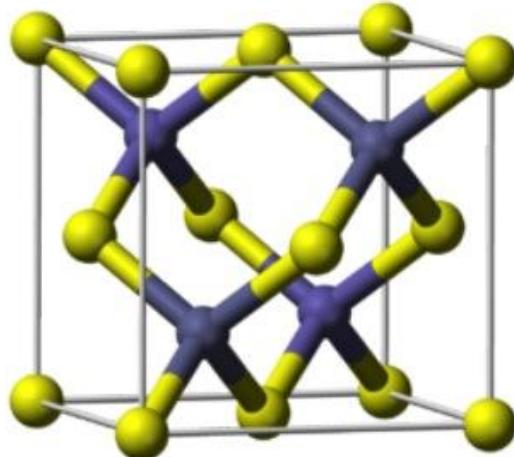


Wurtzite

ZnS

a.

b.



Zinc blende examples

An extremely large number of compounds crystallize in this type of structure including

III-V compounds

AlN, AlP

GaAs, GaP

InP, InAs, InSb

cubic BN

II-VI compounds

ZnSe, ZnTe

CdS, CdSe, CdTe

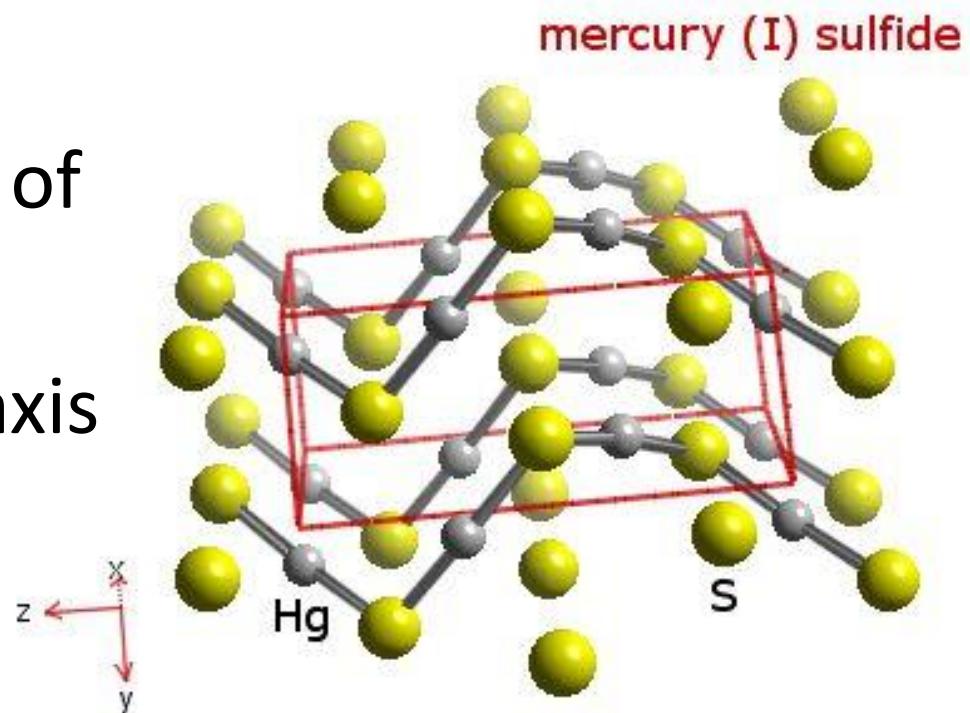
BeS, BeSe, BeTe

SiC

All technologically important materials (electronics) have adamantine structures.

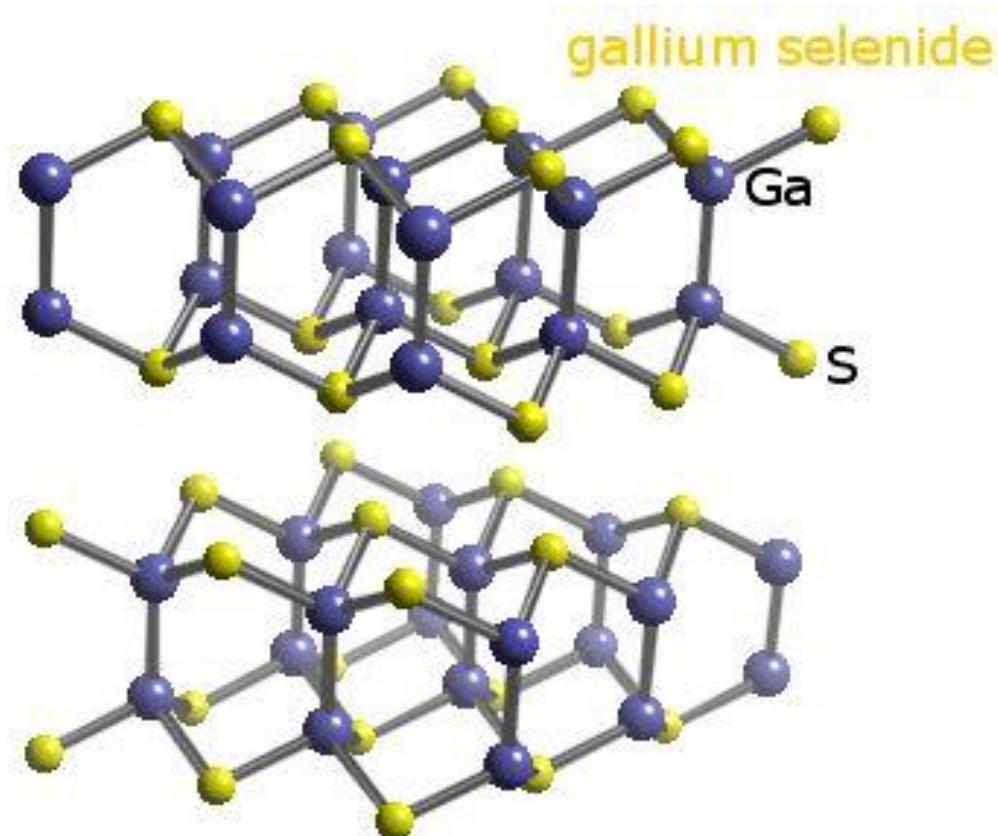
HgS (cinnabar)

- Hexagonal
- High pressure forms of HgSe, HgTe
- Helices along the c-axis
- Aul



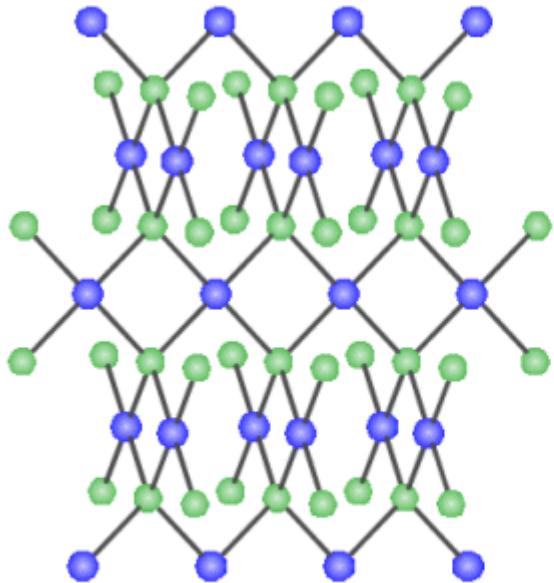
GaS structure

- Layered Hexagonal
- GaSe, InS, InSe
- AlS does not exist



Notice the Ga-Ga bond!

PtS structure



Crystal Structure of
Copper(II) Oxide , CuO

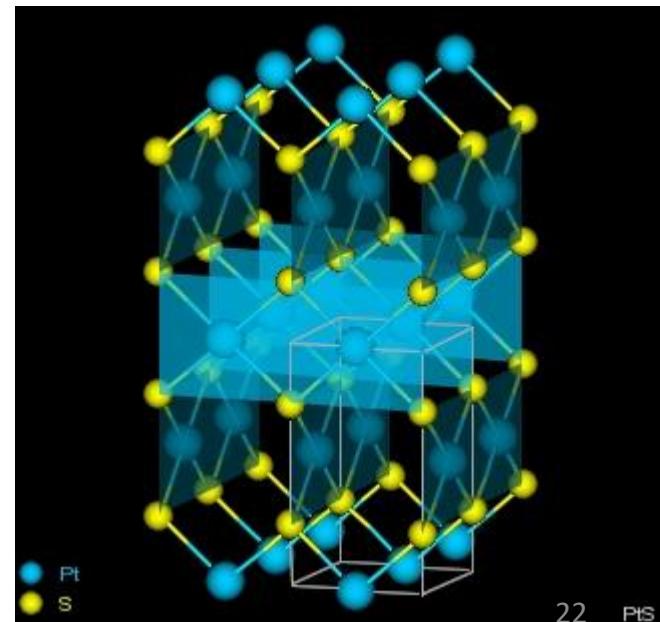
● Cu(II) cation
● Oxide anion

Cu : square planar coordination
oxides : tetrahedral coordination

Note : the CuO₂ ribbons in CuO are actually tilted slightly away from 90° from plane to plane . The model more accurately represents the crystal structure of palladium(II) oxide , PdO.

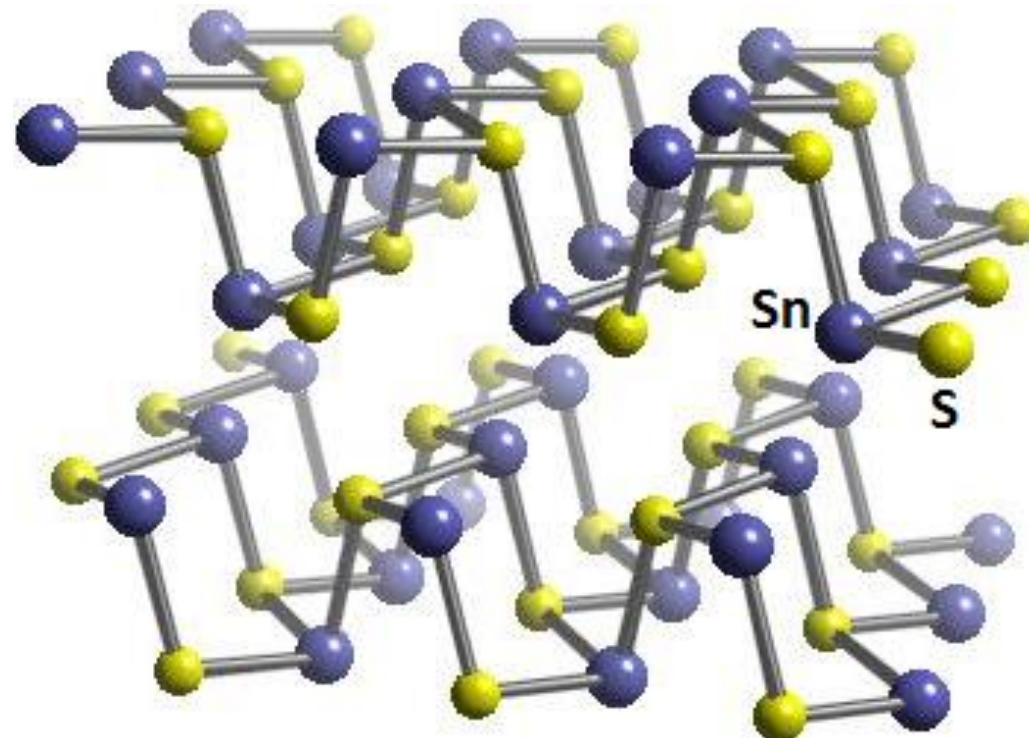
A.F. Wells , "Structural Inorganic Chemistry", third ed. ,
Clarendon Press , Oxford (UK) , 1962 ; Fig. 152(a) , p. 463 .

- Tetragonal
- PtO, PdO
- CuO, AuO (distorted)



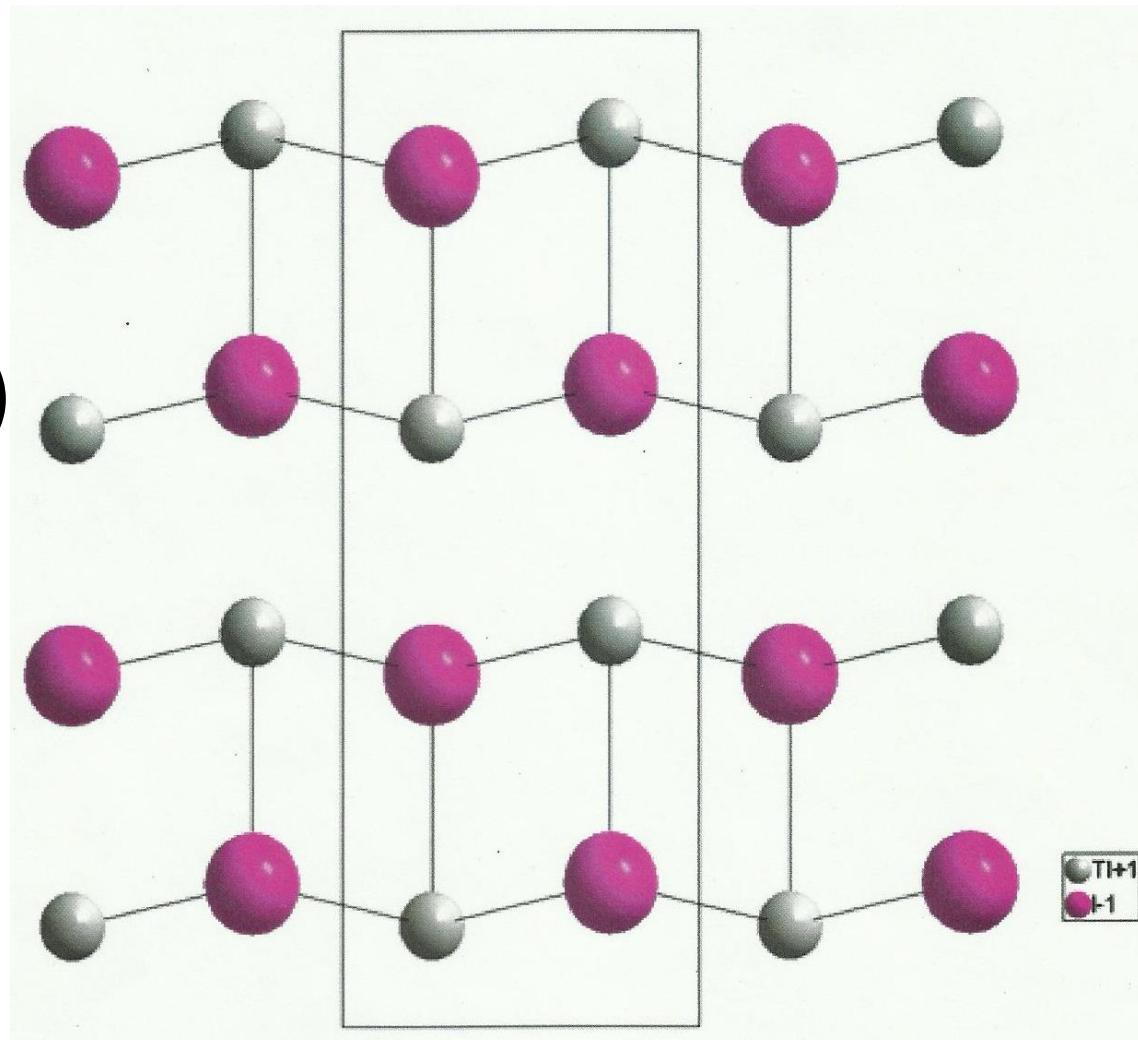
SnS structure

- Orthorhombic
- Derivative of black phosphorus structure
- GeS, GeSe
- SnSe

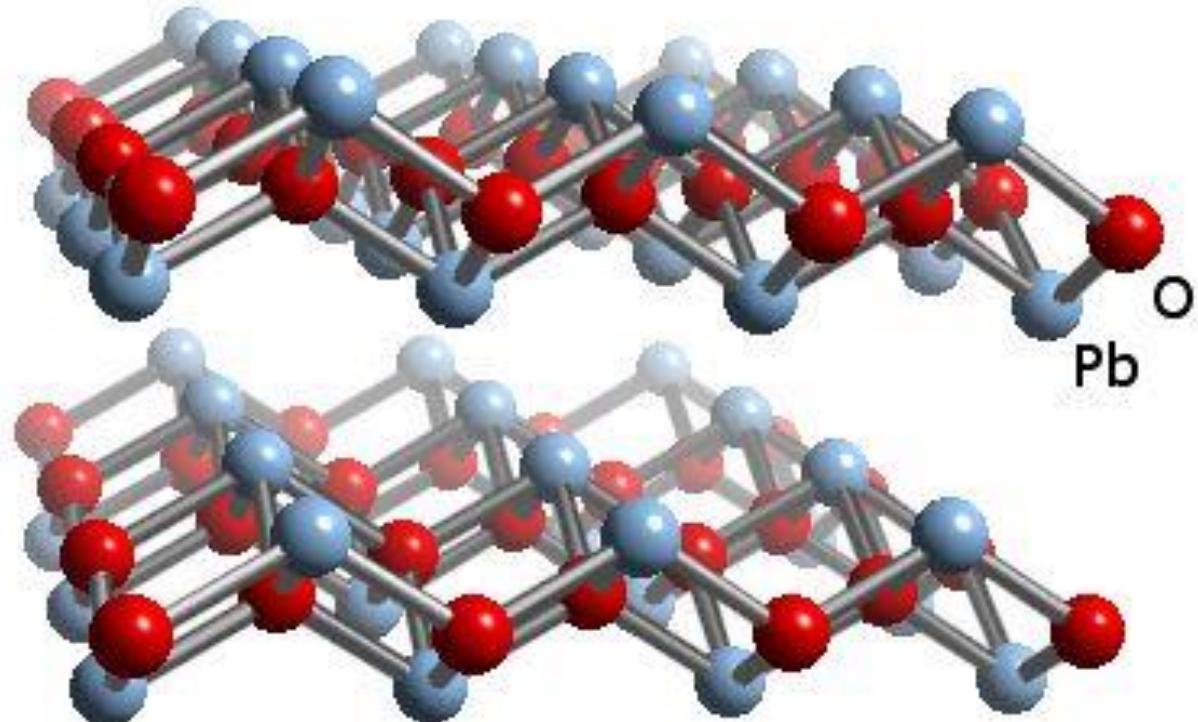


Thallium (I) Iodide

- InBr, InI
- NaOH (anti-PbO)
- KOH
- RbOH
- Not LiOH

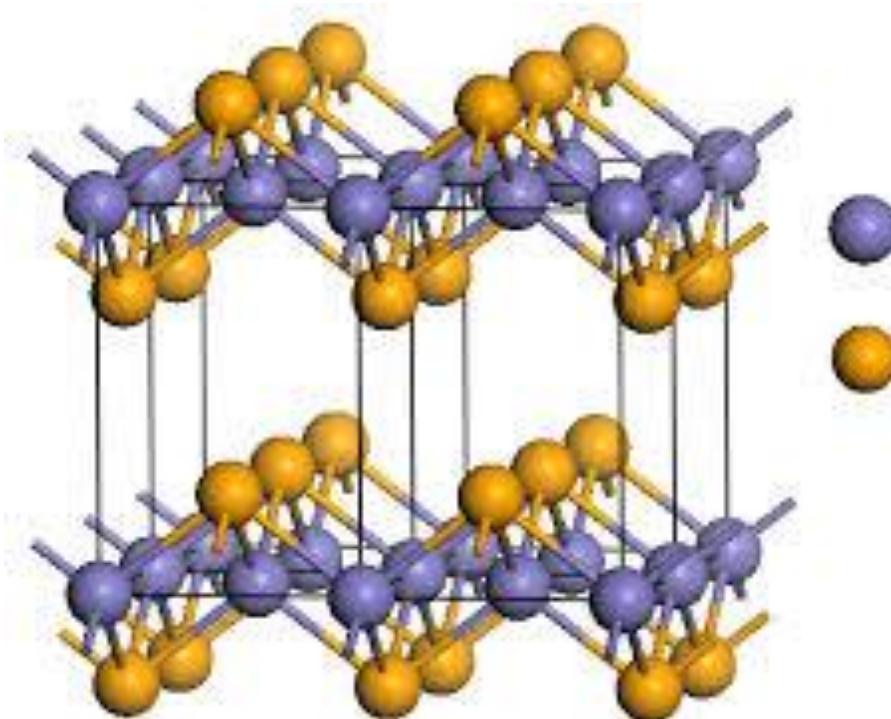


PbO (litharge) structure



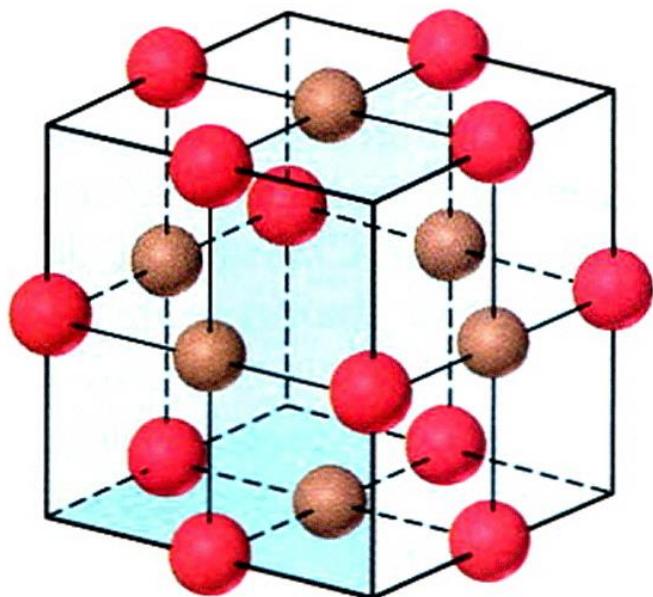
- Tetragonal system
- SnO, LiOH
- FeS (anti)mackinawite
- FeSe

Anti-PbO

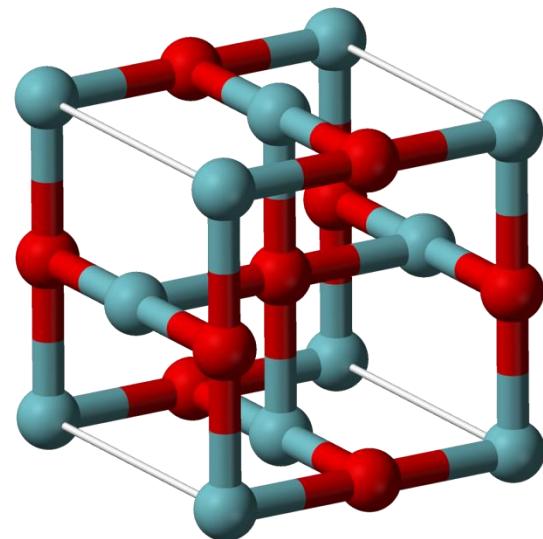
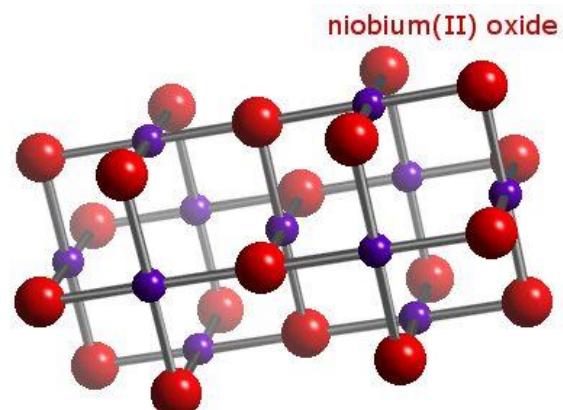


- Tetragonal system
- SnO, LiOH
- FeS (anti)mackinawite

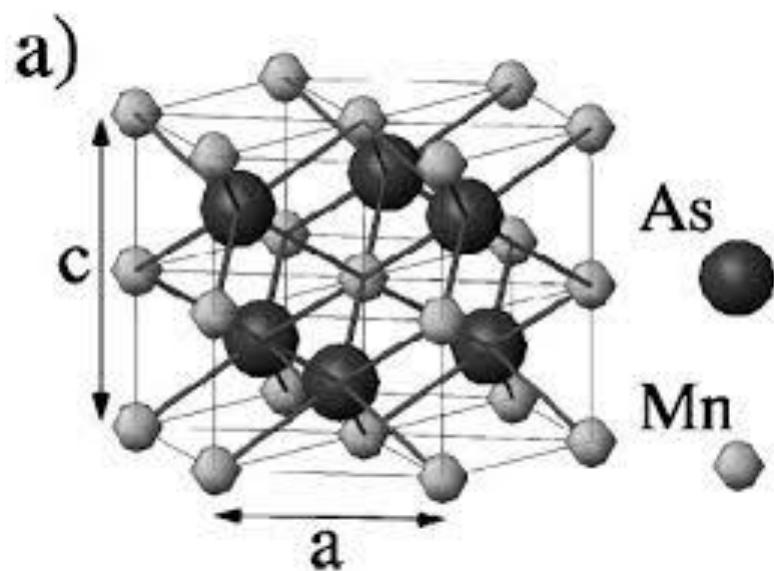
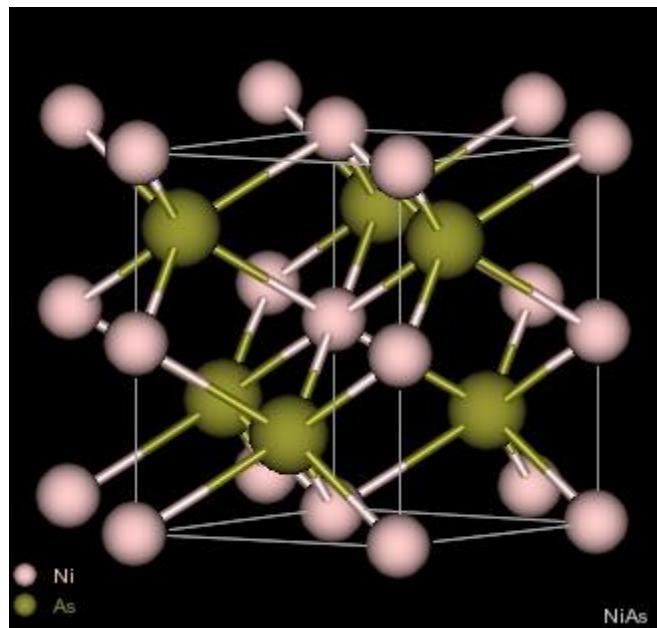
NbO structure



Oxygen
Niobium



NiAs



Solids crystallizing in the NiAs structure type

- CrS, NiS, FeS (Fe_{1-x}S), TiS, MnTe
- CoAs, VP, TiP, NbP, TaP

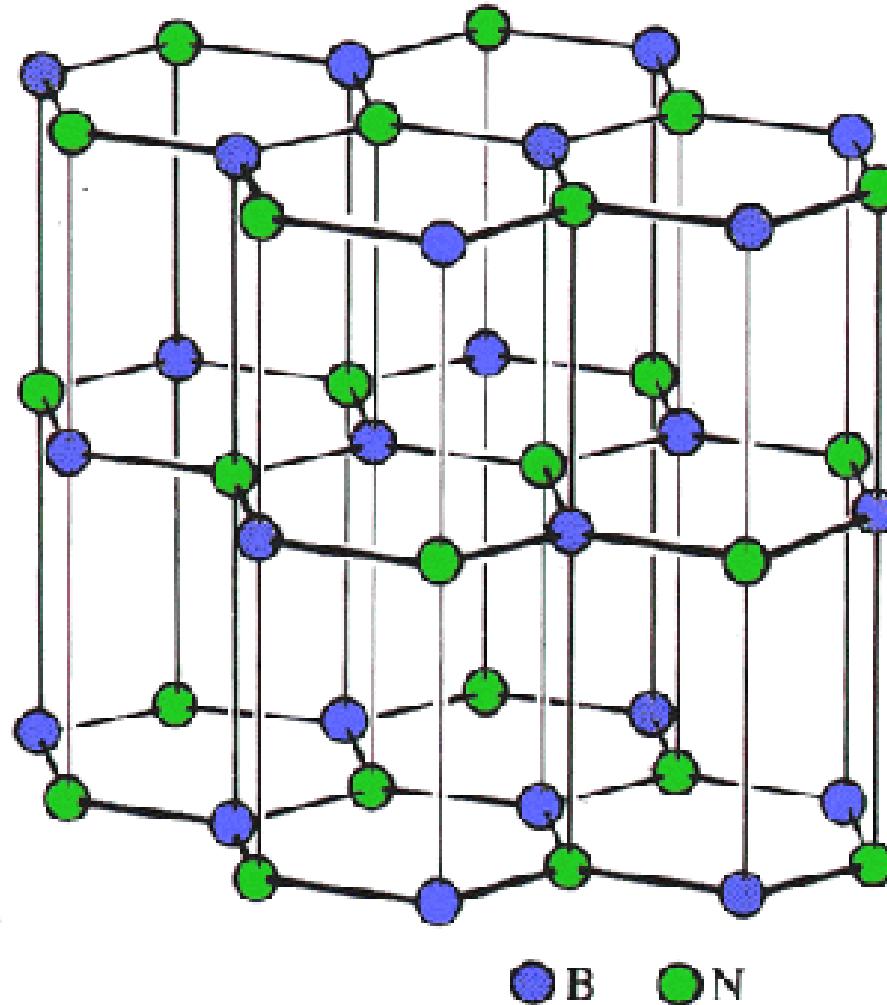
References on NiAs structures:

1. Tremel, W.; Hoffmann, R.; Silvestre, J.; *J. Am. Chem. Soc.* **1986**, *108*, 5178.
2. Kjekshus, A.; Parson, W. B.; *Prog. Solid State Chem.* **1964**, *1*, 83.
3. Hulliger, F.; *Structure and Bonding (Berlin)* **1968**, *4*, 83.

Electronic Structure and Magnetic Properties of Chromium Chalcogenides and Pnictides with NiAs Structure, By: Polesya, Svitlana; Kuhn, Gerhard; Benea, Diana; et al. ZEITSCHRIFT FUR ANORGANISCHE UND ALLGEMEINE CHEMIE Volume: 639 , 2826-2835 Published: DEC 2013

Hexagonal BN: Boron nitride

- Graphite-type structure



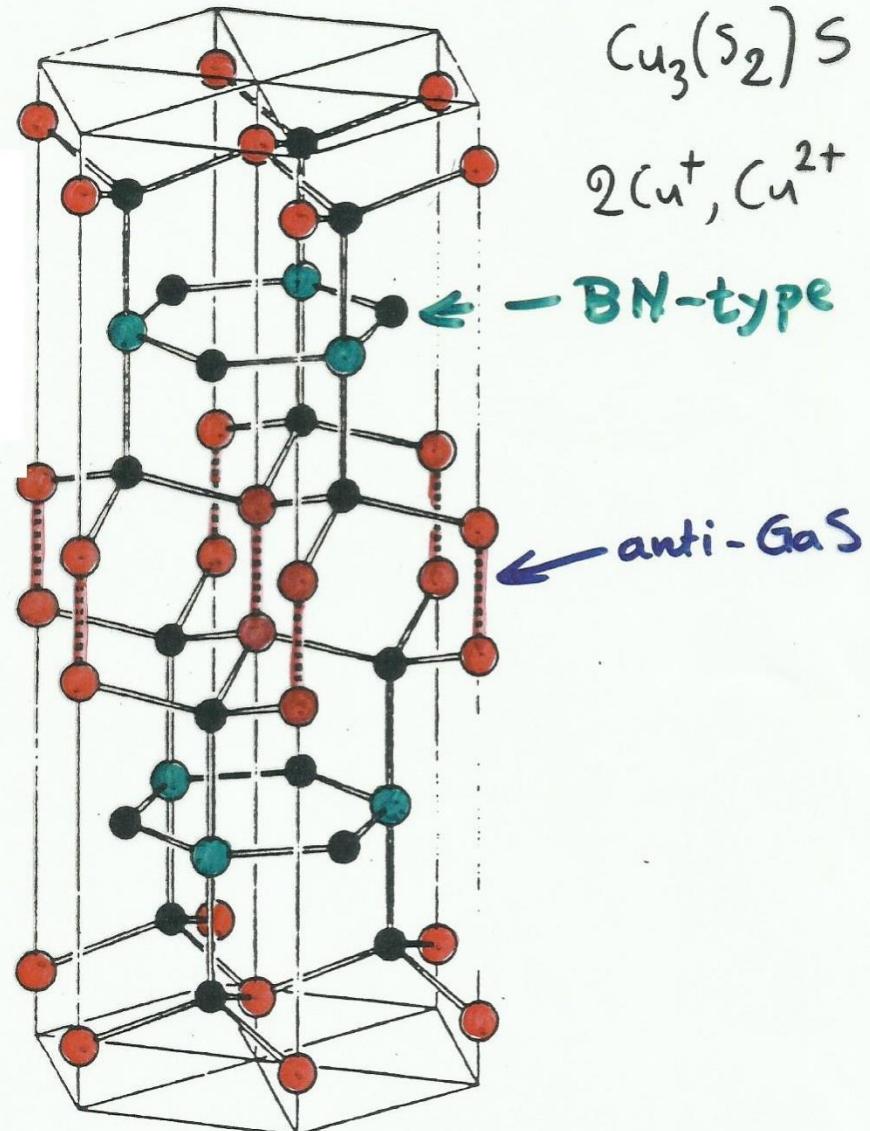
What's in a formula?

CuS Structure

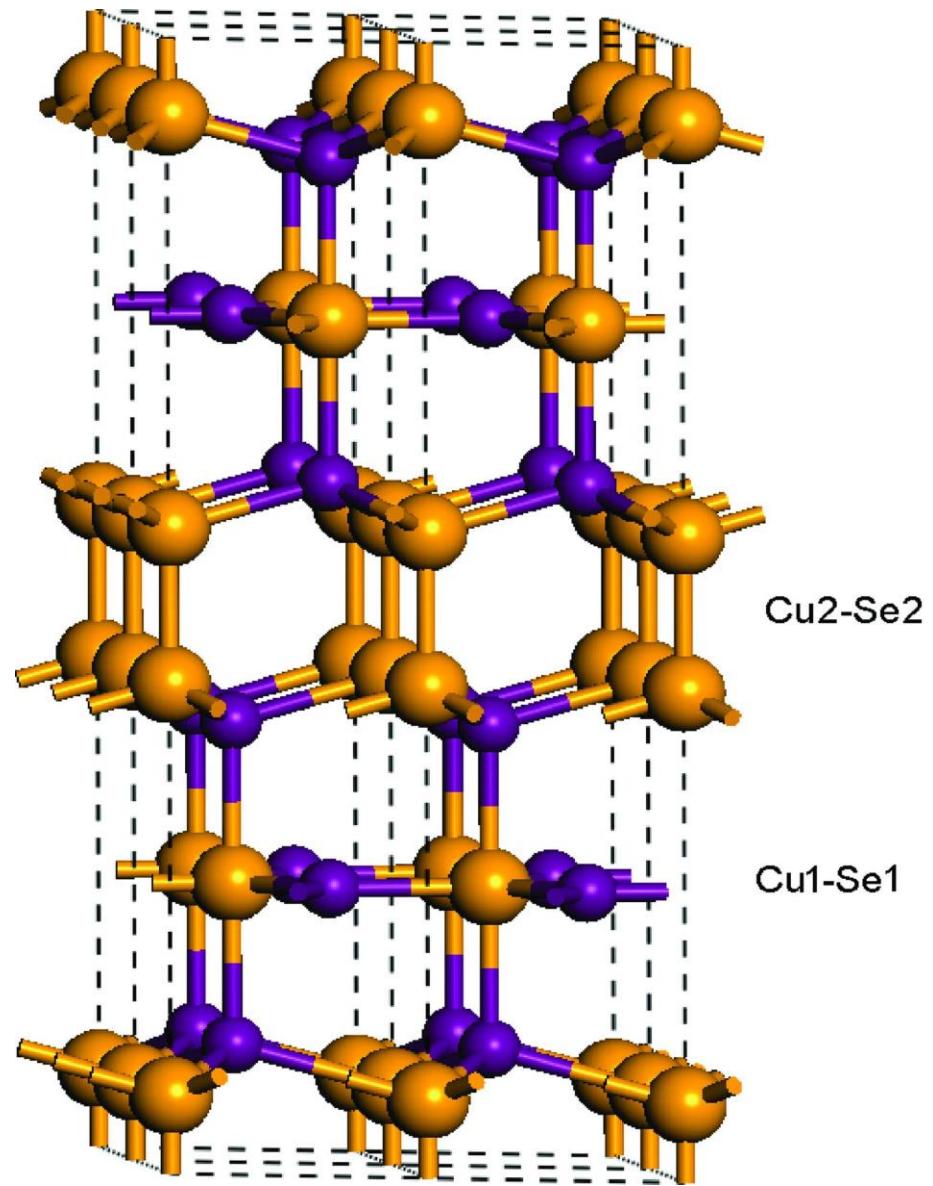
Fig. W-9. The structure of covellite, CuS (solid circles represent Cu, open circles S. The dotted lines indicate covalent S-S bonds.) After Wuensch (1972).

α -CuSe

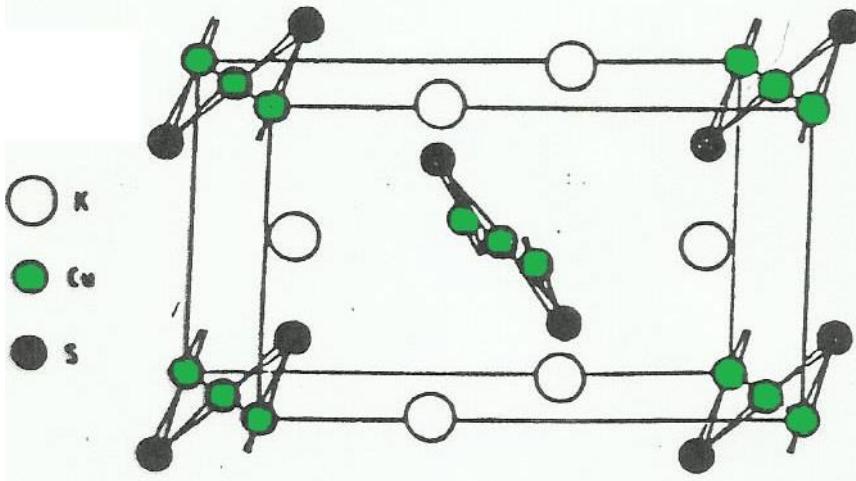
not
CuTe



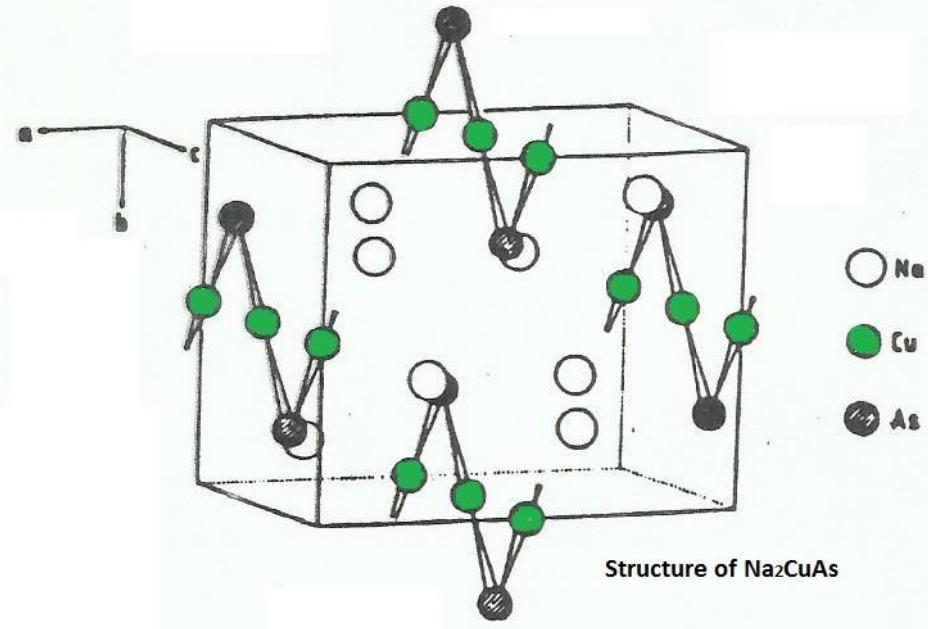
CuS Structure



Some AB-type Cu Compounds



Structure of KCuS



Structure of Na₂CuAs

AuSe structure

